



**TPR**

Department of Transport and Regional Economics  
University of Antwerp

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# Capacity investment size and timing in a port under uncertainty and congestion

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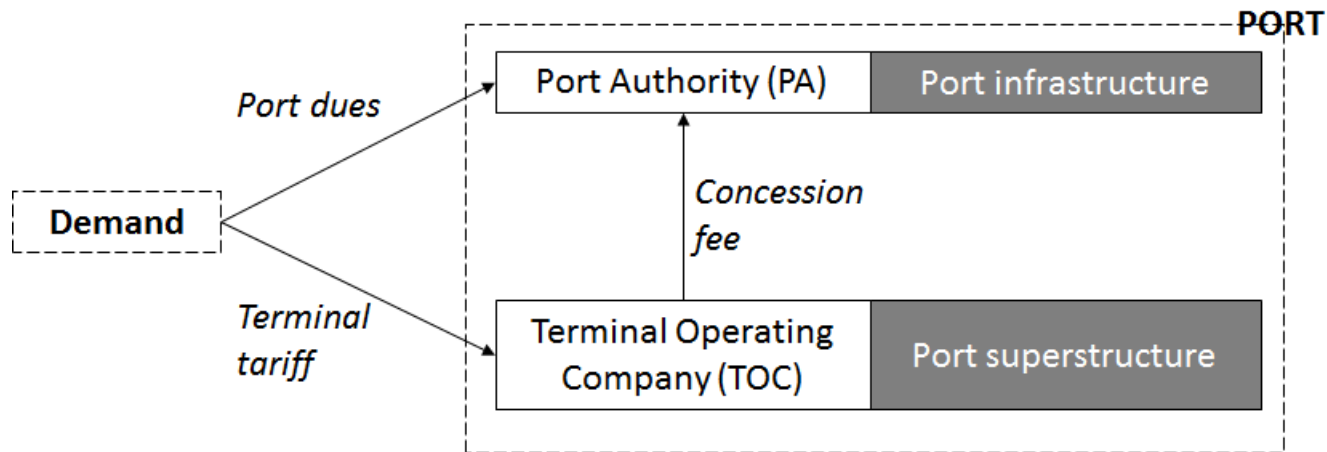
1. Introduction and Problem description
2. Methodology
3. Results
4. Conclusions and Future research

# INTRODUCTION AND PROBLEM DESCRIPTION (1)

- Investments in port capacity:
  - Focus on infrastructure (superstructure needed too)
  - Uncertainty: focus on demand uncertainty
  - Irreversible
  - Large sums of money
- The context:
  - One single investment in new capacity (no expansion)

# INTRODUCTION AND PROBLEM DESCRIPTION (2)

- Port structure:
  - PA vs TOC
  - Privately vs Publically held



Legend:    Port actor    Investment outlay    *Revenue Source* →

# INTRODUCTION AND PROBLEM DESCRIPTION (3)

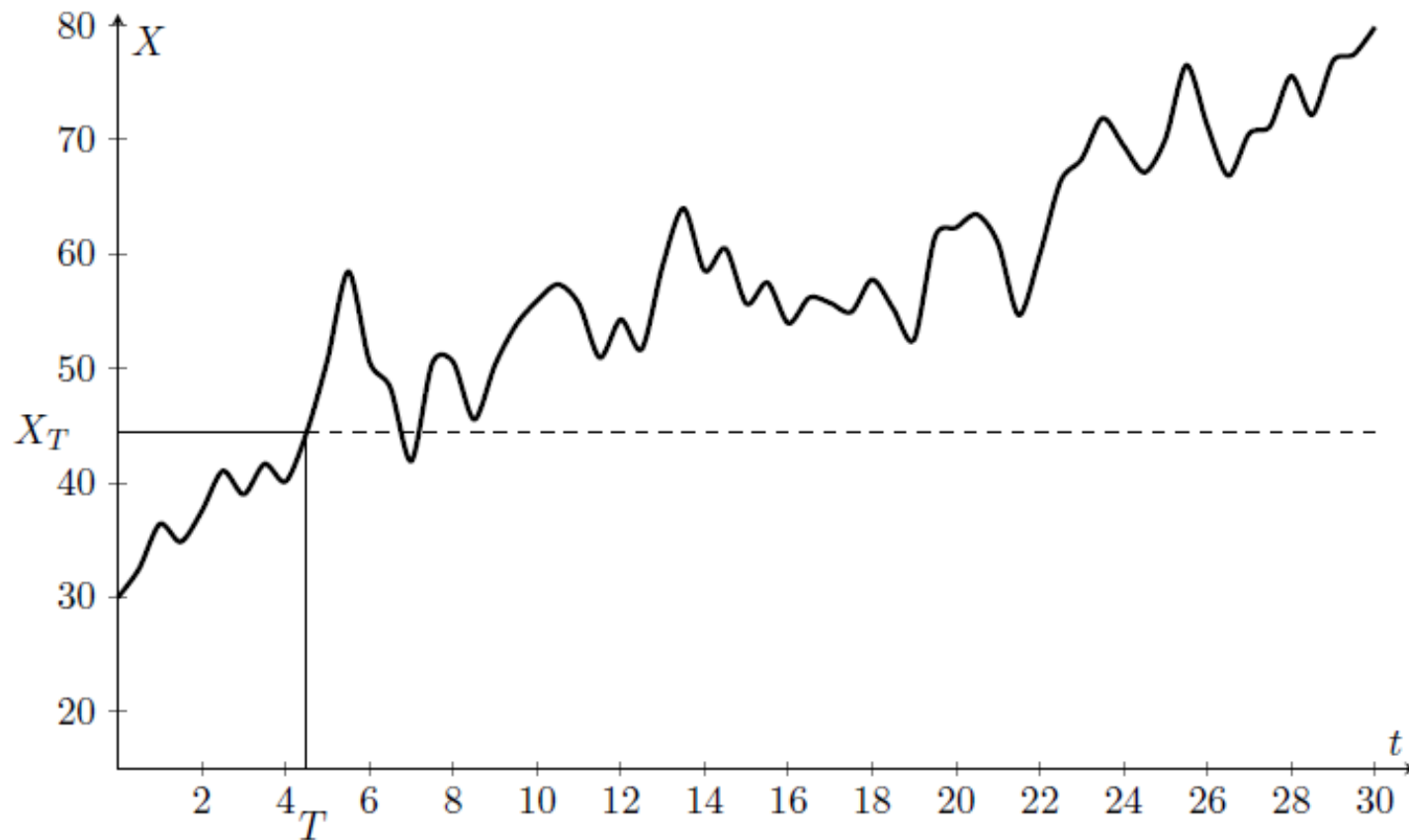
- Trade-off in port capacity
  - **Undercapacity**: waiting times  $\sim$  congestion cost
  - **Overcapacity**: too high investment cost

# METHODOLOGY (1)

- Real options to value flexibility:
  - Size and timing of investment
  - Output flexibility

# METHODOLOGY (2)

- Price:  $p(t) = X(t) - Bq(t)$  :  $X$  = intercept,  $q$  = throughput
- GBM for  $X$  (timing parameter):  $dX(t) = \mu X(t)dt + \sigma X(t)dZ(t)$





# METHODOLOGY (3)

- Model includes congestion cost:  $A \frac{X}{B} \left( \frac{q}{K} \right)^2$   
(adds to literature)
- $K$  = total capacity
- $q/K$  = occupation rate
- $X/B$  = maximal demanded throughput
- $A$  = monetary scaling factor (expression of aversion to waiting time)

# METHODOLOGY (4)

- Multiple actors:
  - Split **income, operational and investment cost** between PA and TOC with shares
  - Concession fee = % of TOC operational  $\pi$

- Public PA:

$$\text{Local benefits } LB = \pi_{PA} + \lambda q$$

$$\lambda (= 0.4) = \text{spillover benefit per unit } q$$

$$\text{Social Welfare } SW = LB + CS$$

$$CS = \text{consumer surplus, i.e. } Bq^2/2$$

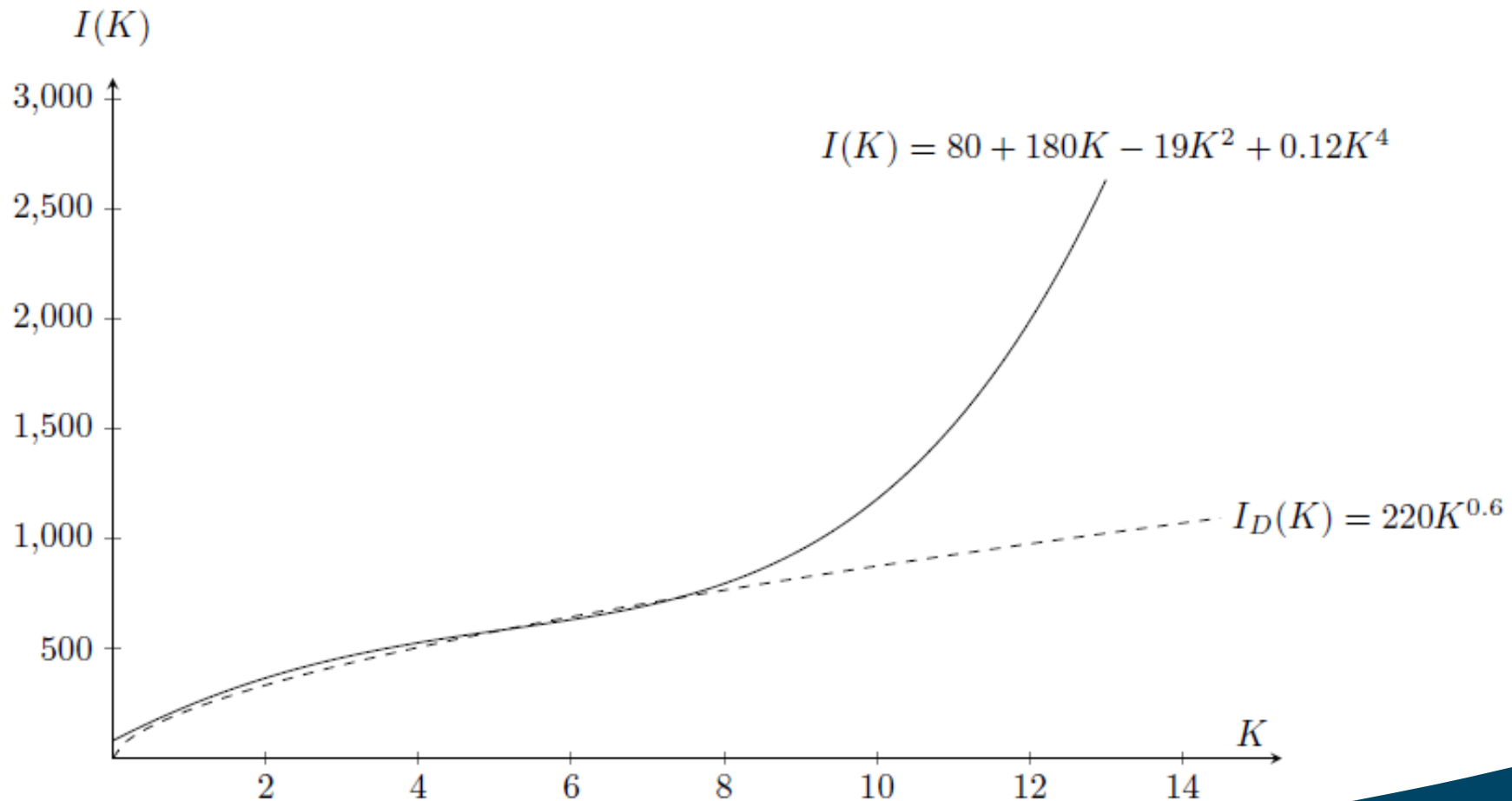
$$\text{PA objective function } \Pi_{PA} = (1 - s_L - s_G) \cdot \pi_{PA} + s_L \cdot LB + s_G \cdot SW$$

$$s_L (\in [0; 1]) = \text{share of PA owned by local government}$$

$$s_G (\in [0; 1]) = \text{share of PA owned by central government}$$

# METHODOLOGY (5)

- Investment function: economies of scale + boundary



# METHODOLOGY (6)

- Optimal  $q$  as a function of  $X(+)$  and  $K(+)$ ,  $K$  is upper limit
- Dynamic programming:
  - Bellman equation and Itô's Lemma:
  - Find discounted sum of cash flows = project value

# METHODOLOGY (7)

- Maximising the option to find optimal  $X(K/+)$ :

$$F(X) = \max\{e^{-rdt}\mathbb{E}(F(X) + dF(X)), \max_K[V(X, K) - I(K)]\}$$

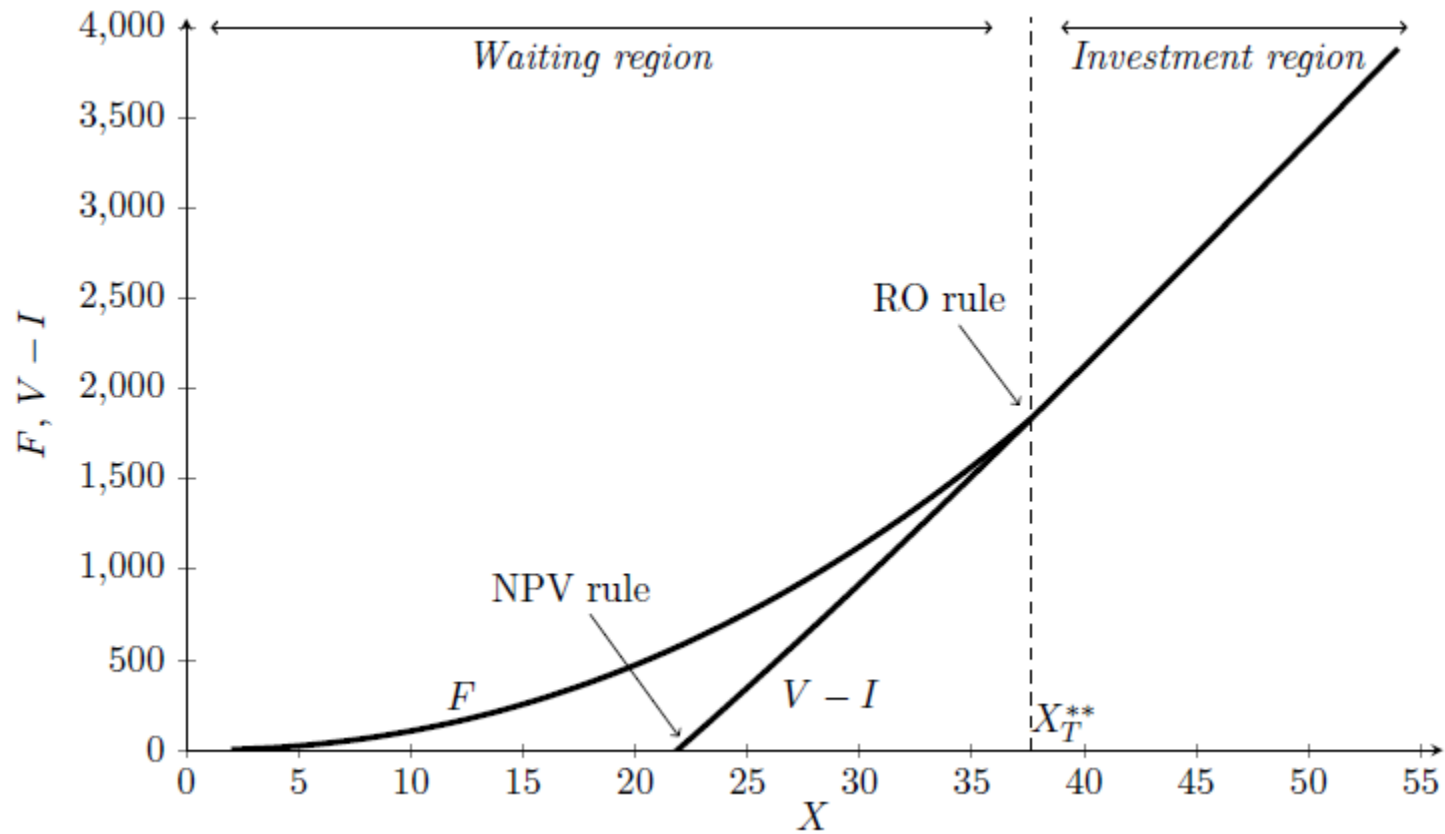
- Optimal  $K(X/+)$ :  $v(X, K) - \frac{dI(K)}{dK} = 0$

- Joint optimum:

- Timing (X, threshold) and size (K, capacity)

# METHODOLOGY (8)

- RO output graphically



# METHODOLOGY (9)

- Stepwise approach for TOC and PA:
  1. Find  $q^{opt}$  for TOC (determines throughput)
  2. Find project  $V$  for TOC
  3. Option value:  $(X, K)$  for TOC
  4. Find project  $V$  for PA (taking  $q^{opt}$ )
  5. Option value:  $(X, K)$  for PA
  6. Determine or negotiate joint decision

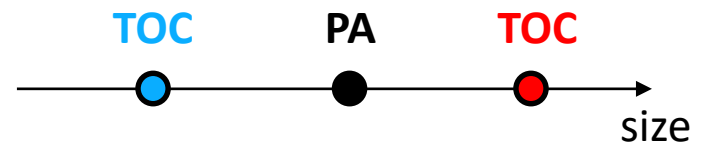
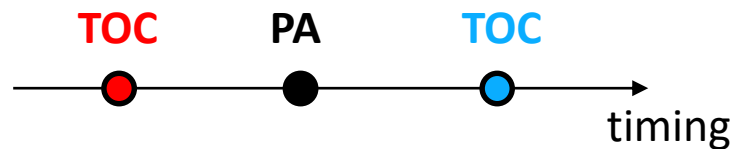
# RESULTS (1)

- Positive relationship between size and timing
- More demand **uncertainty**: Bigger, Later investment
- Higher cost of **congestion**: idem
- Higher **operational and investment** cost: idem
- Higher **economic growth**: idem
- More **public money** involved: Earlier investment



## RESULTS (2)

- TOC and PA may have different optimal investment
- Uniform decision required (concession agreement)
  - Negotiation interval
  - Negotiation power



- Concession fee has an impact:
  - Low fee? (PA: later + more,) TOC: earlier + less
  - Fee equaling size or timing of both actors
  - 2 PA strategies (negotiate or force)

# CONCLUSIONS AND FUTURE RESEARCH

- Impact of uncertainty
- The role of congestion aversion in a port
- Multiple actors and owners
  
- Expand models:
  - Competition (Game theory)
  - Port expansion and Time to build
  - Phased investment

# Thank you for your attention!

## Questions?

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